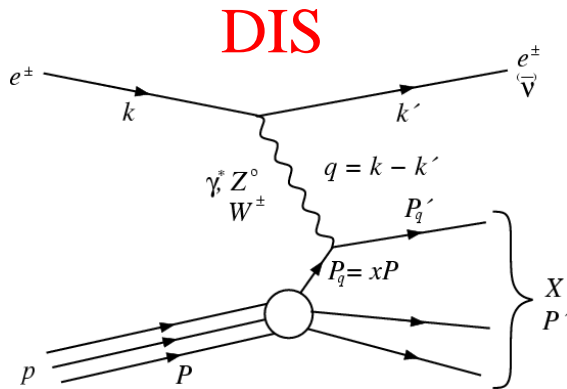


# Experimental Review of Unpolarised Structure Functions

**Vladimir Chekelian (MPI for Physics, Munich)**

- SF and parton densities
- A few historical remarks
- Recent JLAB and NuTeV results
- HERA results:
  - $F_2$ , gluon,  $\alpha_s$ , jets,  $F_2^{cc}$ ,  $F_2^{bb}$ ,  $F_L$ ,
  - NC&CC at high  $Q^2$ ,  $xF_3$ ,
  - pdf
- First results from HERA II
- Summary

# Unpolarised SF and Parton Densities



## DIS cross section and SF

$$\frac{d^2\sigma_{NC}^{e^\pm p}}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} Y_\pm \left[ F_2 - \frac{y^2}{Y_+} F_L \mp \frac{Y_-}{Y_+} xF_3 \right], Y_\pm = 1 \pm (1-y)^2$$

in QPM:  $F_2(x, Q^2) = x \sum A_i(q_i + \bar{q}_i)$

$$xF_3(x, Q^2) = x \sum B_i(q_i - \bar{q}_i)$$

$$F_L = F_2 - 2xF_1 = 0$$

$Q^2 = -q^2$       *virtuality of  $\gamma^*$ ,  $Z^\circ$ ,  $W^\pm$*

$x = Q^2/2(pq)$       *Bjorken scaling variable*

$y = (Pq)/(pk)$       *inelasticity*

## Factorisation

$$\sigma_{DIS} \sim \hat{\sigma} \otimes pdf(x)$$

$\hat{\sigma}$  – perturbative QCD cross section

*pdf* - universal parton distribution functions

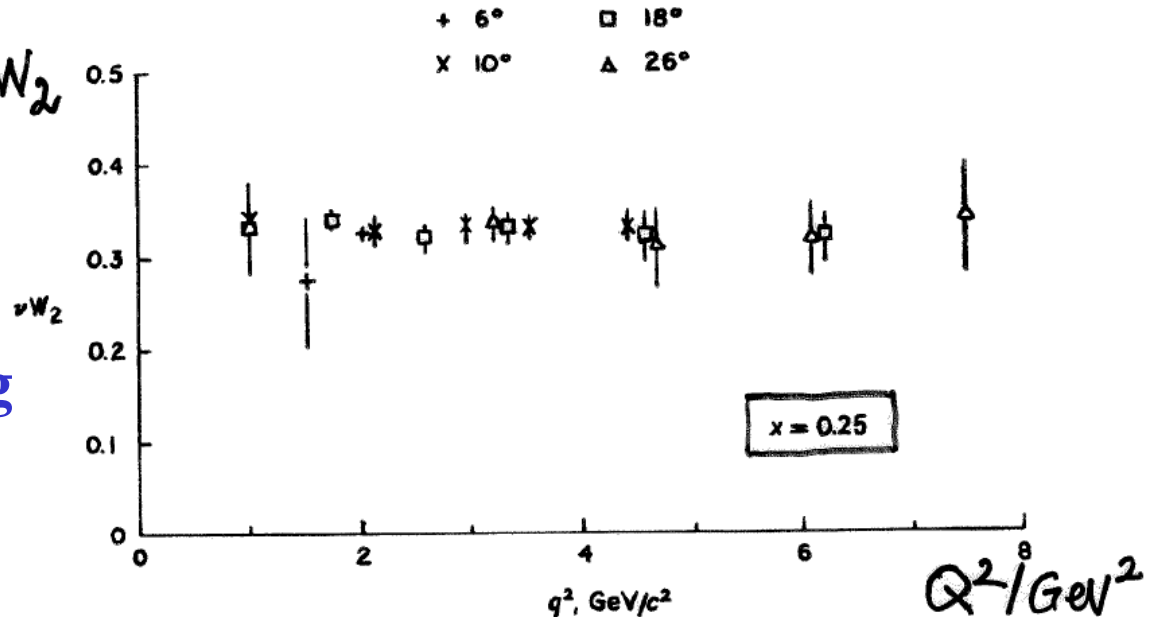
## QCD evolution (NLO, NNLO)

DGLAP

BFKL, CCFM

# SF: a few Historical Remarks

1969 SLAC-MIT  $\nu W_2$   
observation that  
the proton SF  
is independent of  $Q^2$   
at fixed Bjorken  $x$   
→ **Bjorken scaling**  
**QPM**



1974 - ... SLAC, EMC, BCDMS, NMC, CDHS, CHARM, CCFR, ...  
logarithmic  $Q^2$  dependence of  $F_2(x, Q^2)$  established in  $e/\mu/\nu N$   
scattering experiments  
→ **scaling violations**  
**QCD**

# 2004 Nobel Prize in Physics for the Discovery of Asymptotic Freedom

David Gross, David Politzer, Frank Wilczek



## Selected Publications of Frank Wilczek, with Brief Commentary

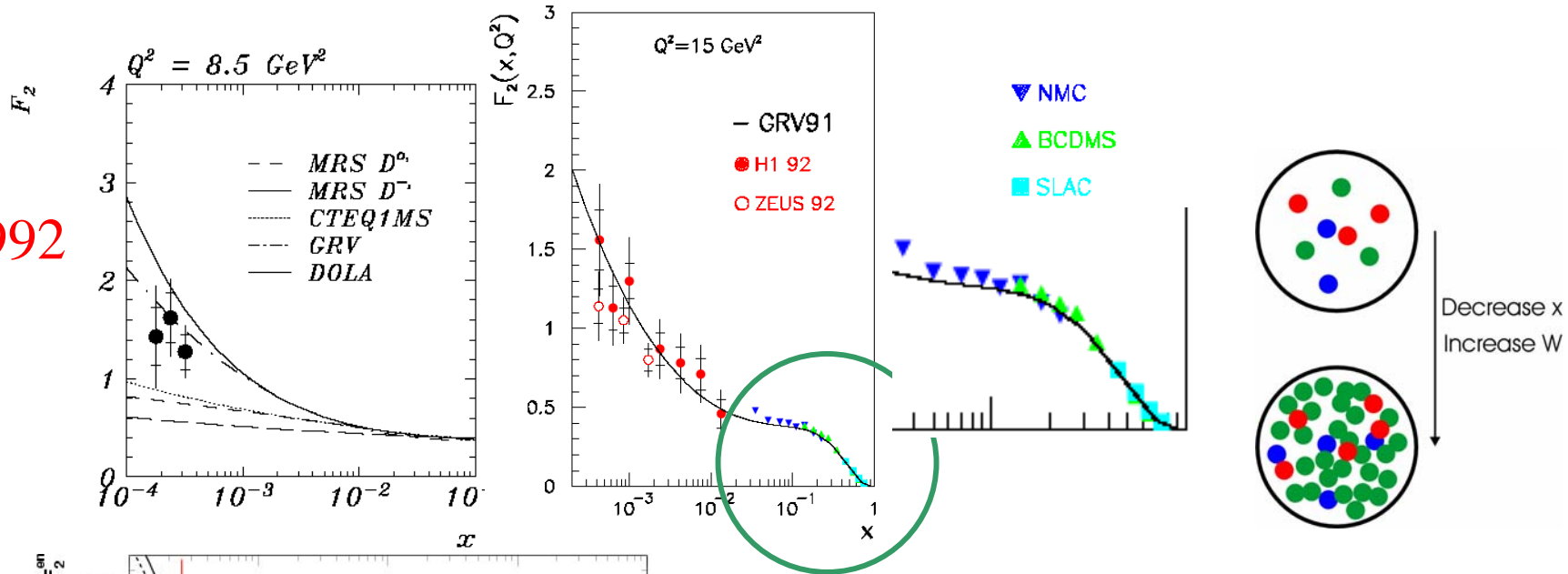
[http://web.mit.edu/physics/facultyandstaff/faculty\\_documents/wilczek\\_select\\_pubs.pdf](http://web.mit.edu/physics/facultyandstaff/faculty_documents/wilczek_select_pubs.pdf)

### QCD: Foundational Papers

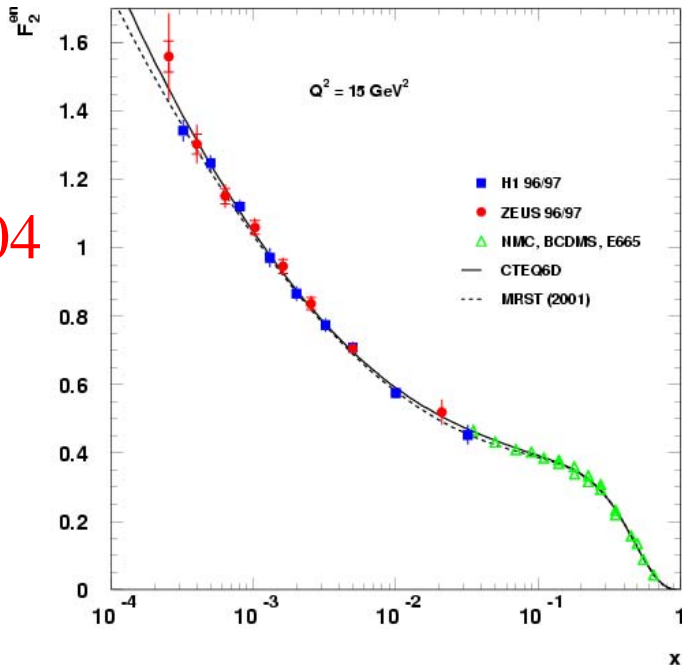
... in the fifth and sixth papers further experimental consequences, regarding the pointwise evolution of structure functions, were derived. **The most dramatic of these, that proton viewed at ever higher resolution would appear more and more as field energy (soft glue), was only clearly verified at HERA twenty years later. ...**

# Rise of $F_2$ to Low $x$ at HERA

1992



2004



the first HERA data:

- discovery of the  $F_2$  rise at low  $x$

driven by gluon !

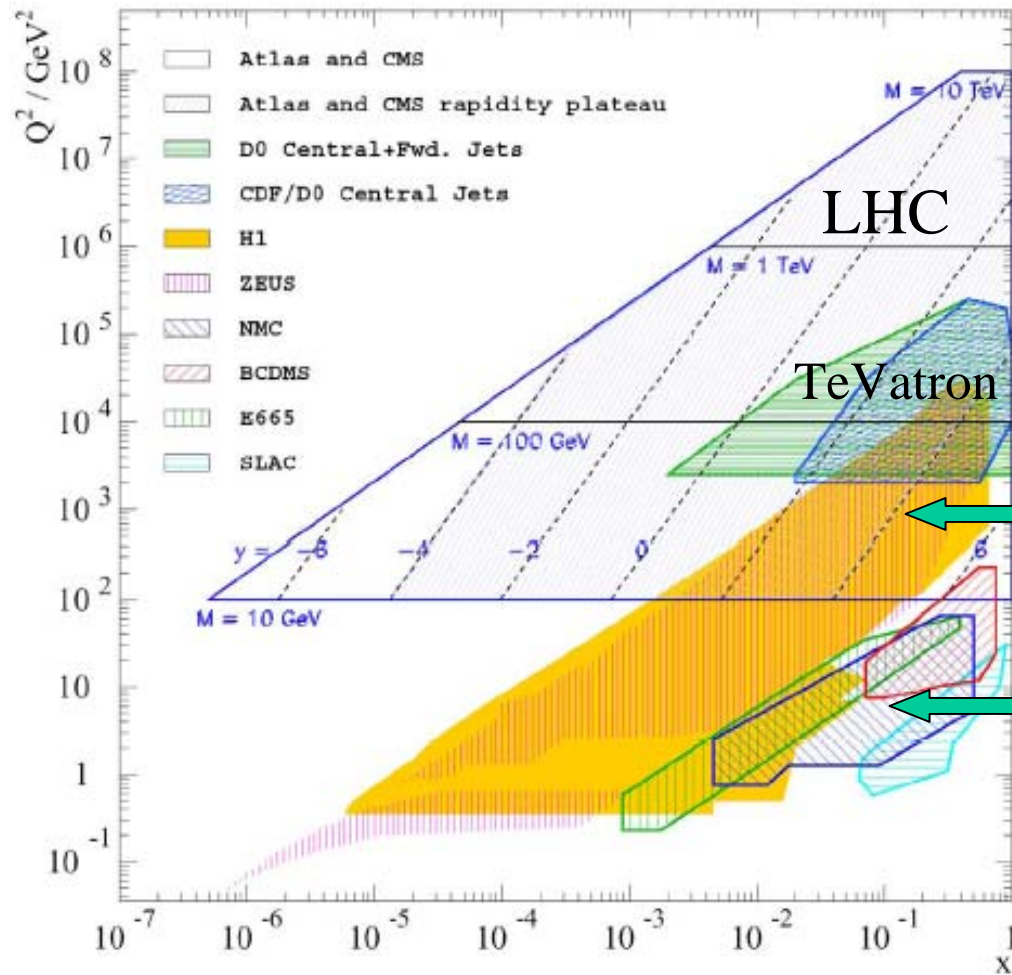
can not rise forever

search for new gluon dynamics  
(saturation effects, ...)

after 12 years of HERA:

precise data allowing to look for  
smallest deviations

# Kinematic Reach in $Q^2$ and $x$



full HERA  $x$  range is needed for LHC

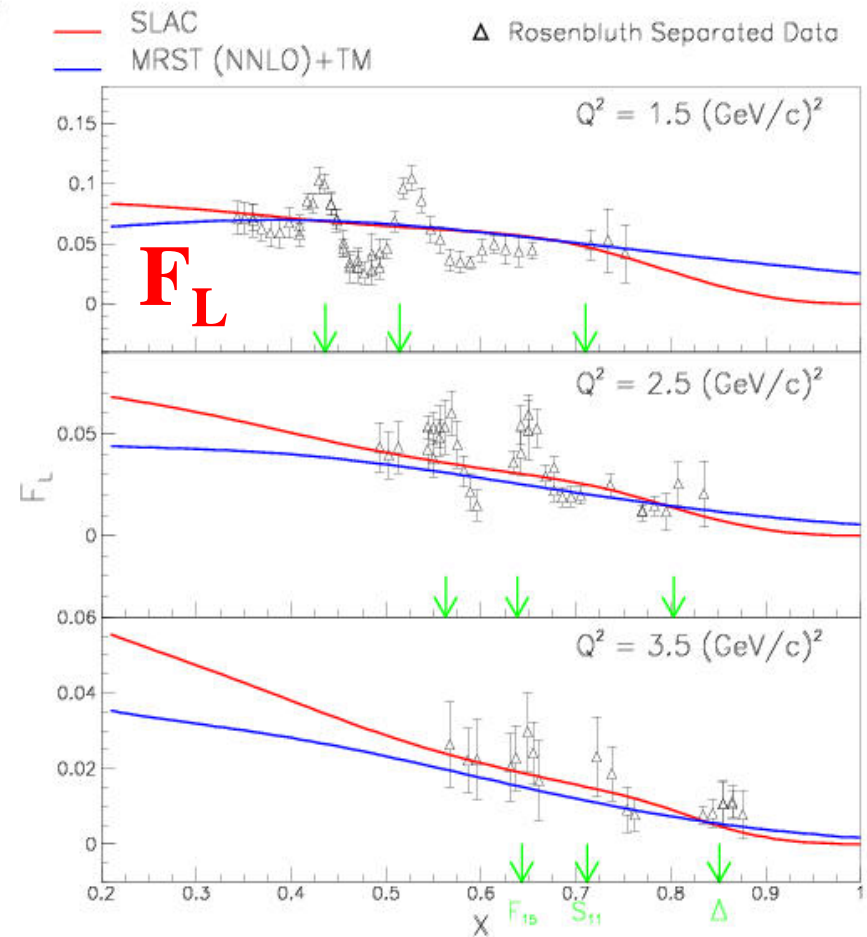
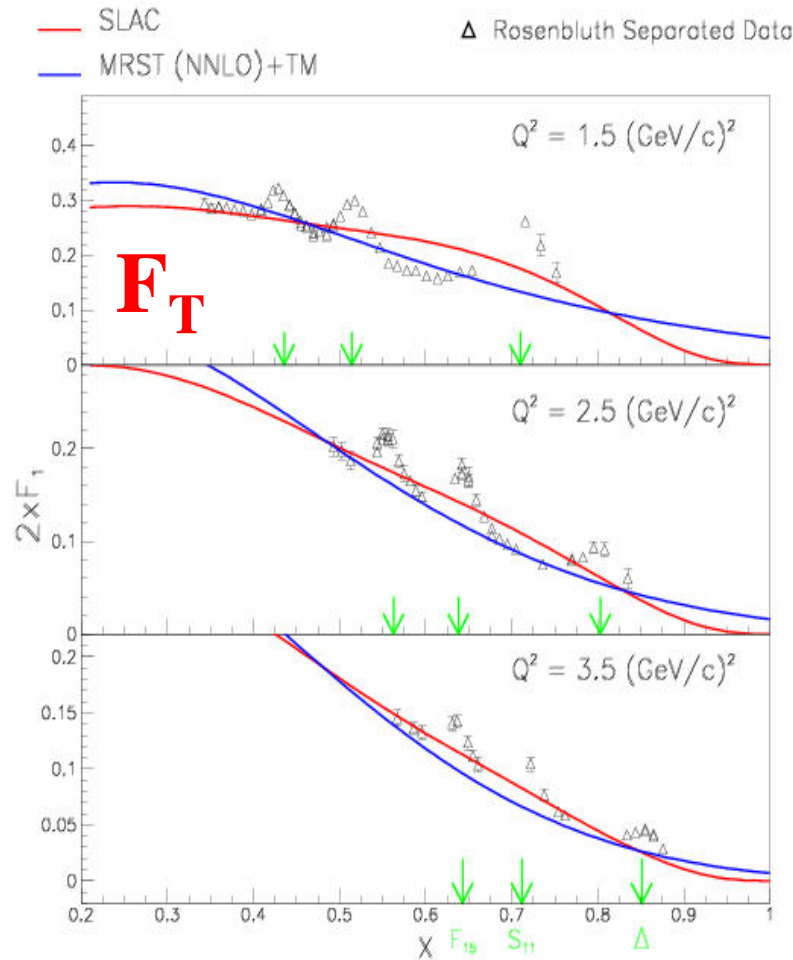
**HERA**

**fixed target experiments**

SLAC, BCDMS, NMC, E665, ...

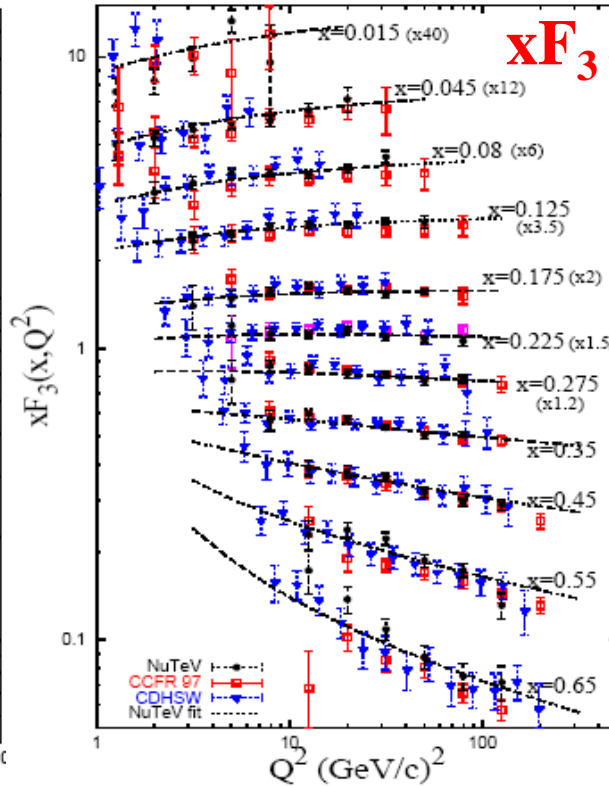
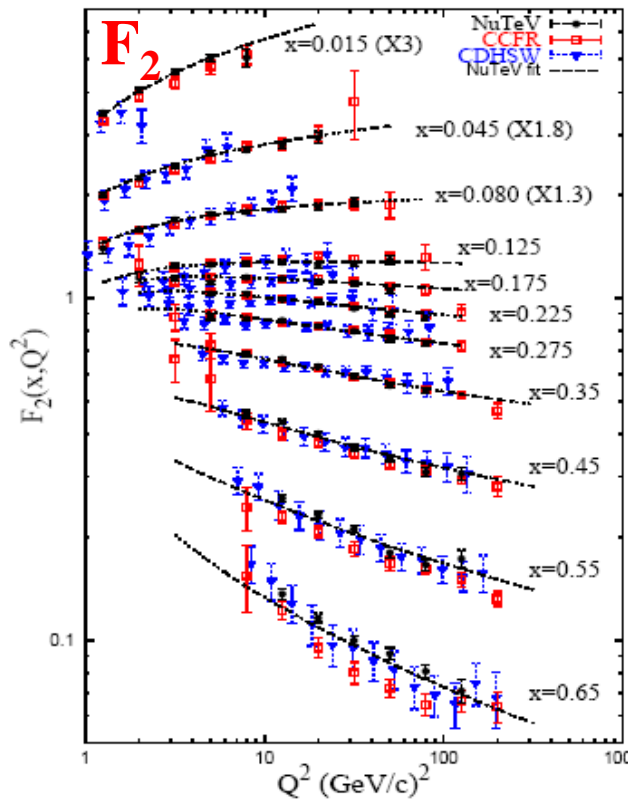
# $F_T$ and $F_L$ in Resonance Region (JLAB E94-110)

$1 < W < 2 \text{ GeV}$



Quark-hadron duality works well for both  $F_T$  and  $F_L$  above  $Q^2 \sim 1.5 \text{ GeV}^2$

# Recent NuTeV Results



$\nu$ -Fe

$$F_2(x, Q^2) = 2x \sum (q_i + \bar{q}_i)$$

$$xF_3(x, Q^2) = 2x \sum (q_i - \bar{q}_i)$$

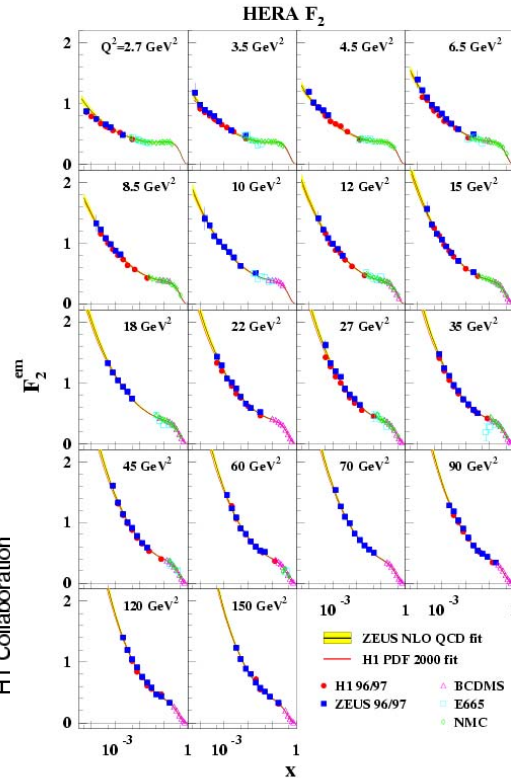
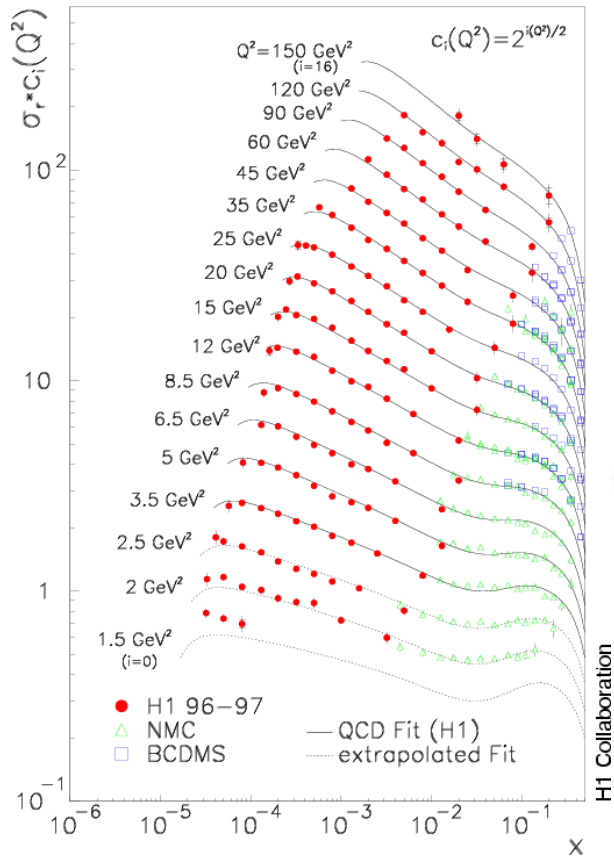
- extended to high  $y$  (low  $x$ )
- most precise measurements of this kind
- half of syst.err. of CCFR

**Strange Sea Asymmetry vs. the “NuTeV Anomaly”:**

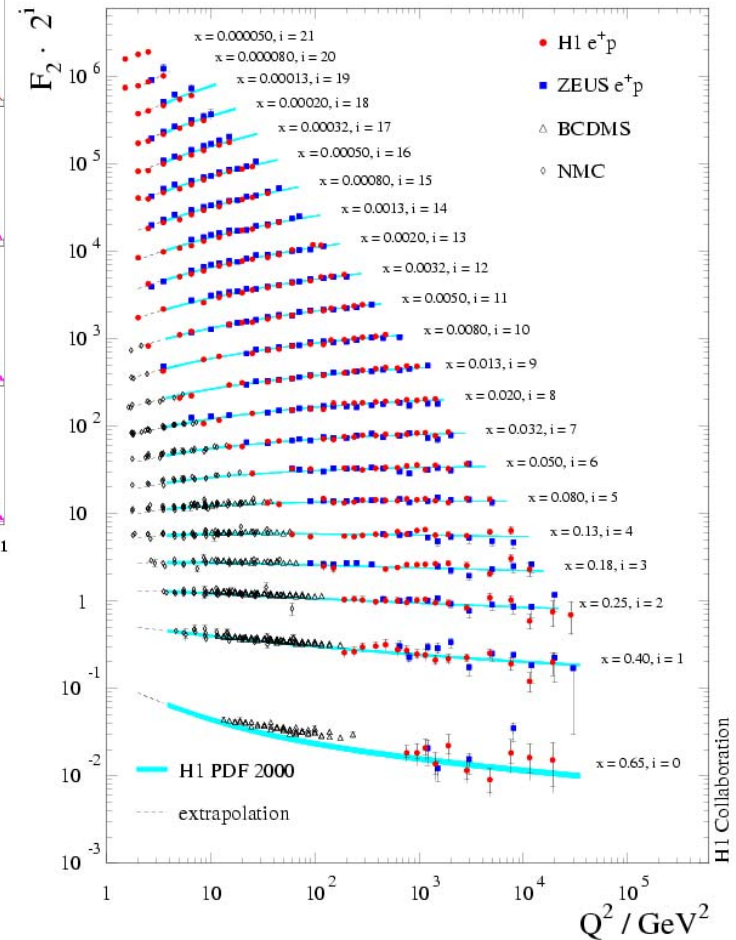
→ see talk of S. Forte



# $F_2(x, Q^2)$ Measurements at HERA



precision data  $\pm 2\text{-}3\%$   
 5 decades in  $x$   
 5 decades in  $Q^2$

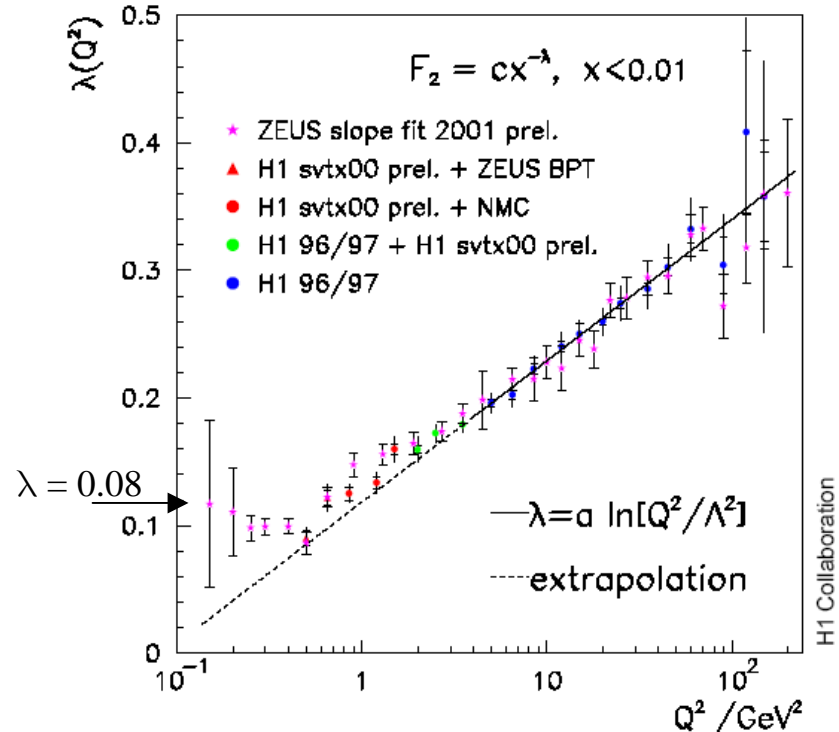
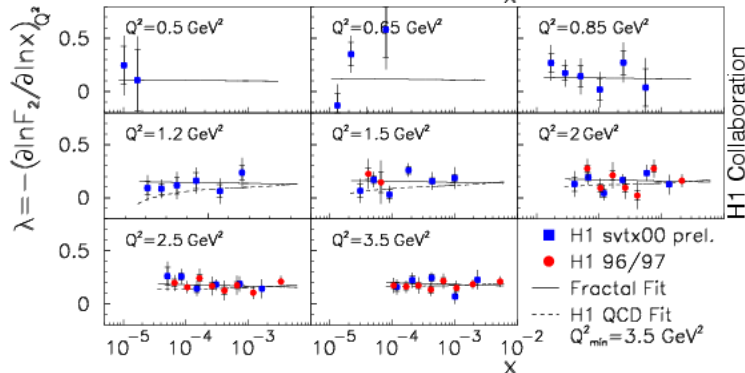
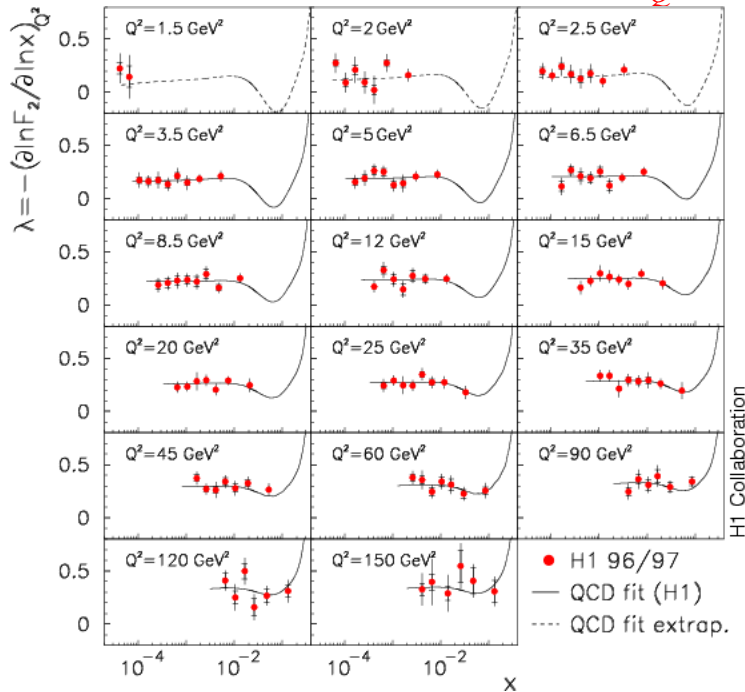


rich possibilities to determine pdfs, test QCD,  
 transition to  $\gamma p$ , search for saturation effects, ...

# Low x at HERA

locally  $\lambda = -(\partial F_2 / \partial \ln x)_{Q^2}$

$\lambda(Q^2)$  from fit  $F_2(x, Q^2) = c(Q^2)x^{-\lambda(Q^2)}$

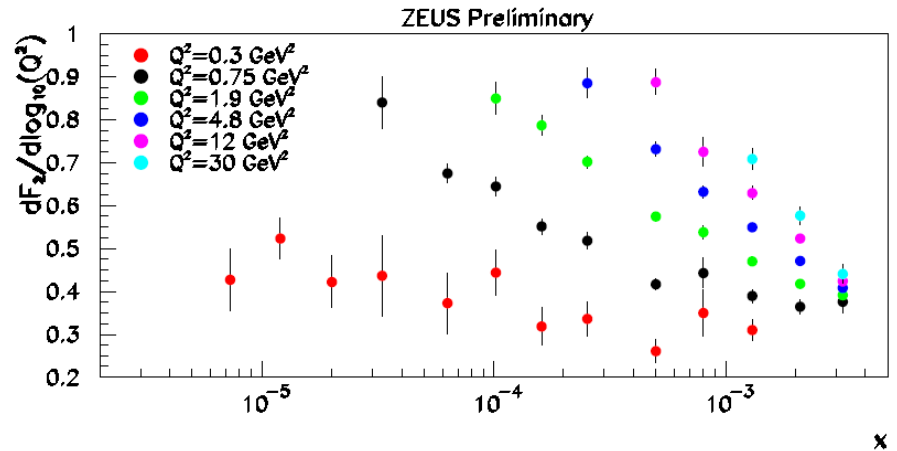
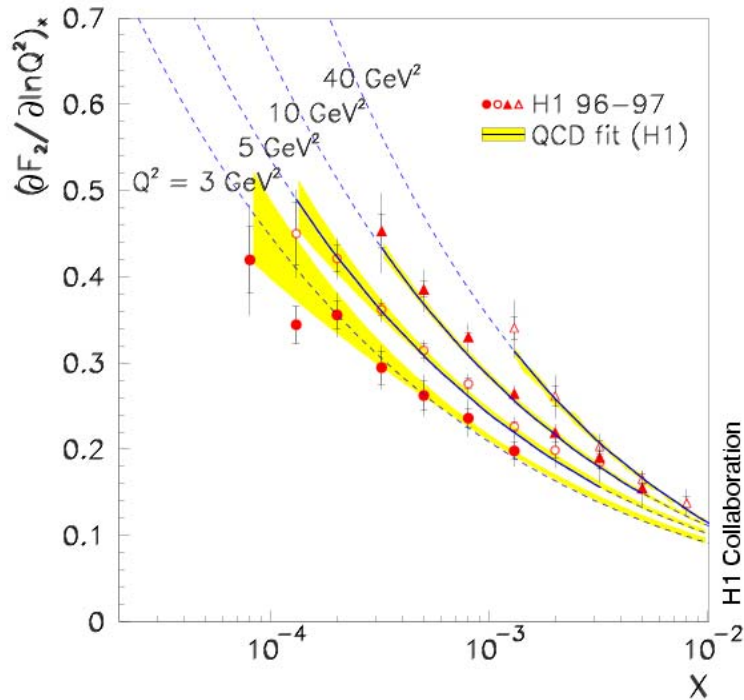


- $\lambda \approx$  constant at fixed  $Q^2$  ( $x < 0.01$ )
- $\lambda(Q^2)$  depends linearly on  $\ln(Q^2)$
- agrees with QCD for  $Q^2 \geq 2 \text{ GeV}^2$
- change of behavior at  $Q^2 \approx 1 \text{ GeV}^2$
- soft pomeron limit  $\lambda = 0.08$  (DL)

no taming of the rise of  $F_2$  towards low  $x$  for  $Q^2 \geq 0.5 \text{ GeV}^2$

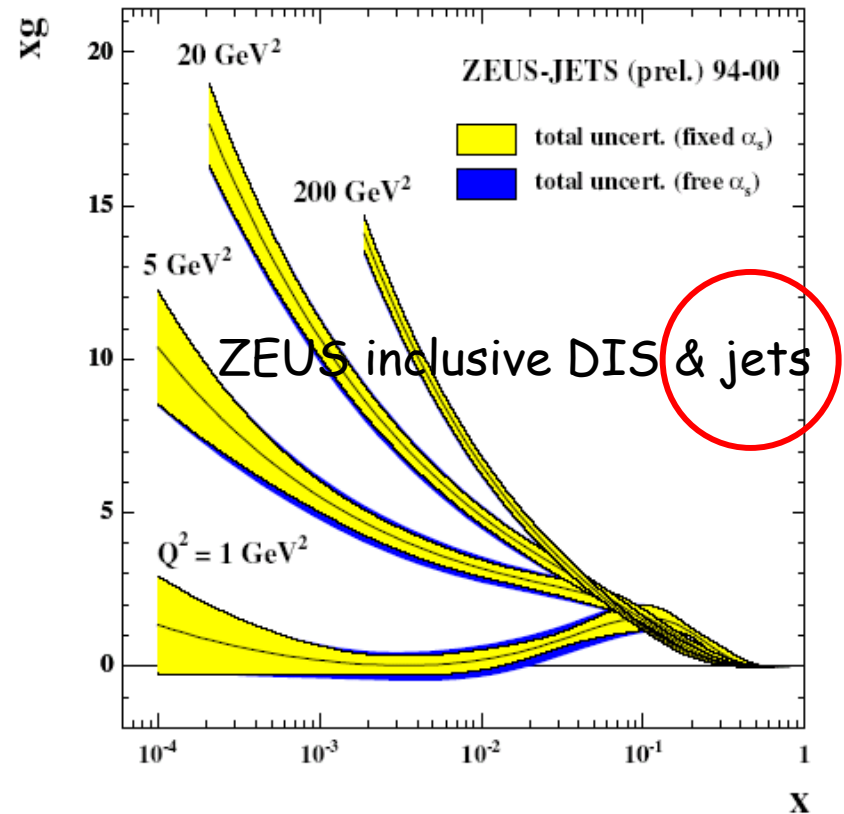
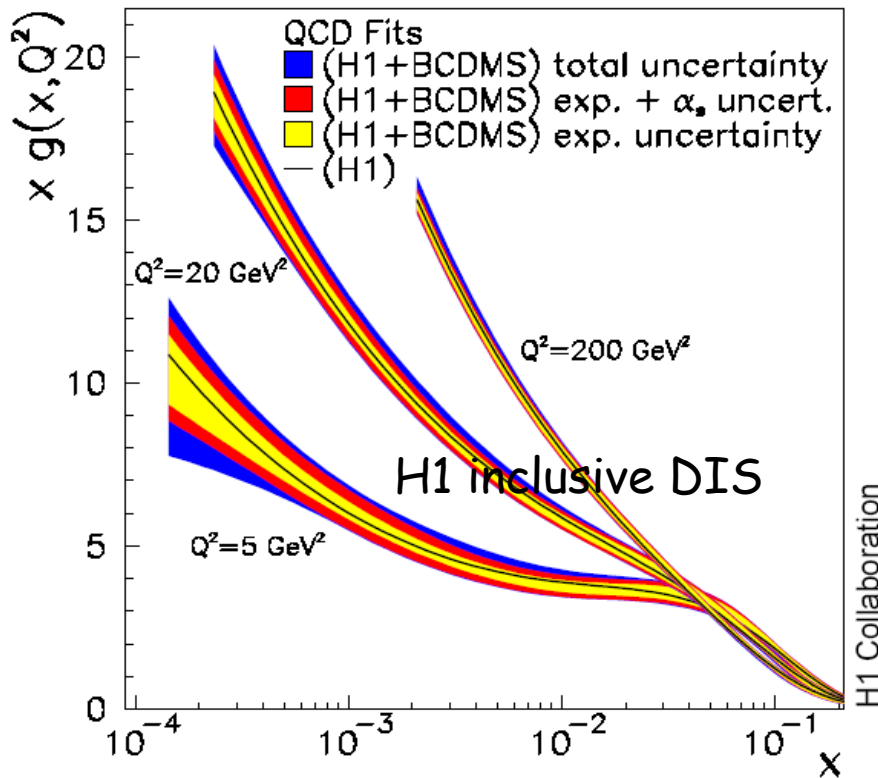
# Scaling Violations at Low x

driven by gluon  $(\partial F_2 / \partial \ln Q^2)_x \propto \alpha_s(Q^2) x g(2x, Q^2)$  (LO)



- continuous rise towards low  $x$
- consistent with QCD fit ( $Q^2 \geq 3 \text{ GeV}^2$ )
- no evidence for new gluon dynamics

# Gluon Density from HERA NLO QCD Fits



**Gluon** → scaling violations

pin down the gluon allows to resolve correlation of  $xg \leftrightarrow \alpha_s$   
charm treatment important

at  $Q^2 \sim 1 \text{ GeV}^2$  the gluon distribution becomes very small →  $xg$  is NOT an observable

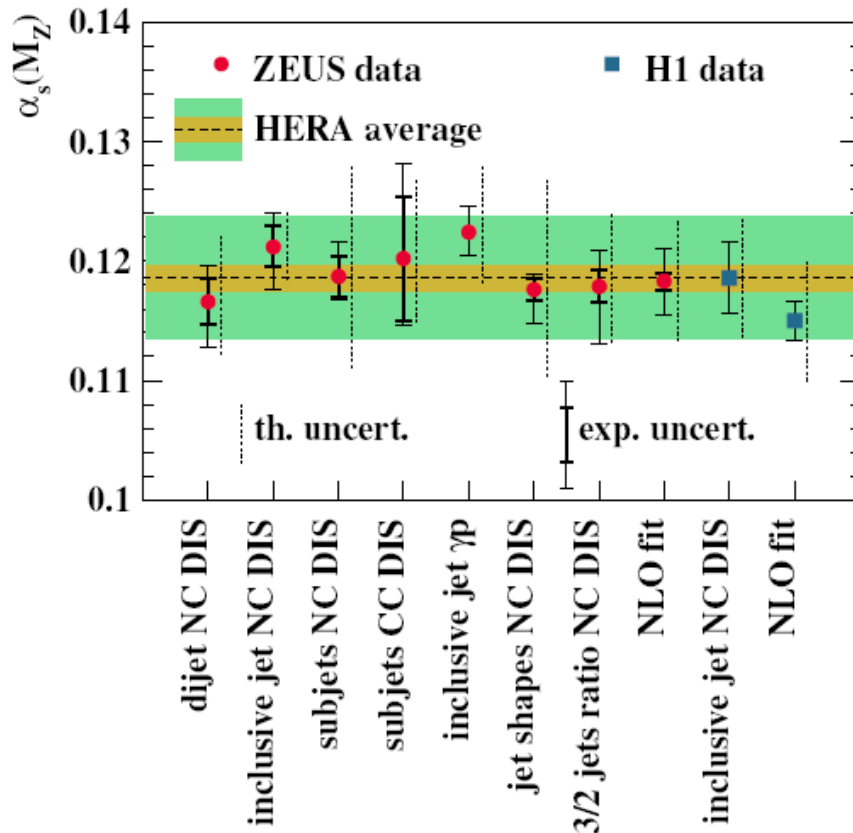
**Gluon** → jets, heavy flavours,  $F_L(x, Q^2)$  directly sensitive to  $xg$

# Strong Coupling from HERA NLO QCD Fits and Jets

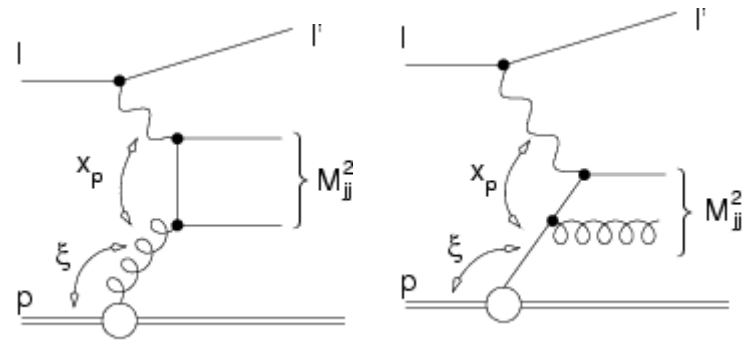
From scaling violations:

$$\alpha_s(M_Z^2) = 0.1209 \pm 0.0015(\text{exp}) \pm_{0.0049}^{0.0048}(\text{thy}) - \text{ZEUS}$$

$$\alpha_s(M_Z^2) = 0.1160 \pm 0.0016(\text{exp}) \pm_{0.0046}^{0.0058}(\text{thy}) - \text{H1}$$



Jets



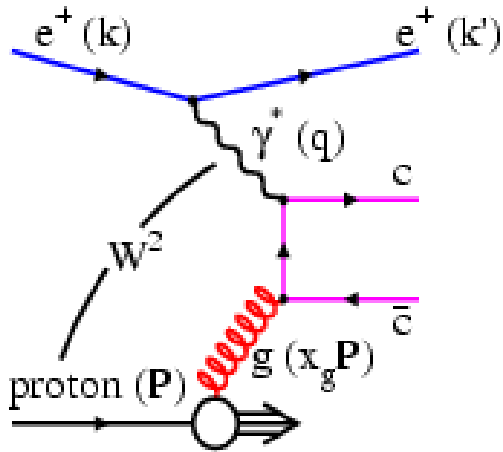
*HERA(prel.)*

$$\alpha_s(M_Z^2) = 0.1186 \pm 0.0011(\text{exp}) \pm 0.005(\text{thy})$$

- small exper. error  $\sim 1\%$
- theory error in NNLO expected to be 3 times smaller

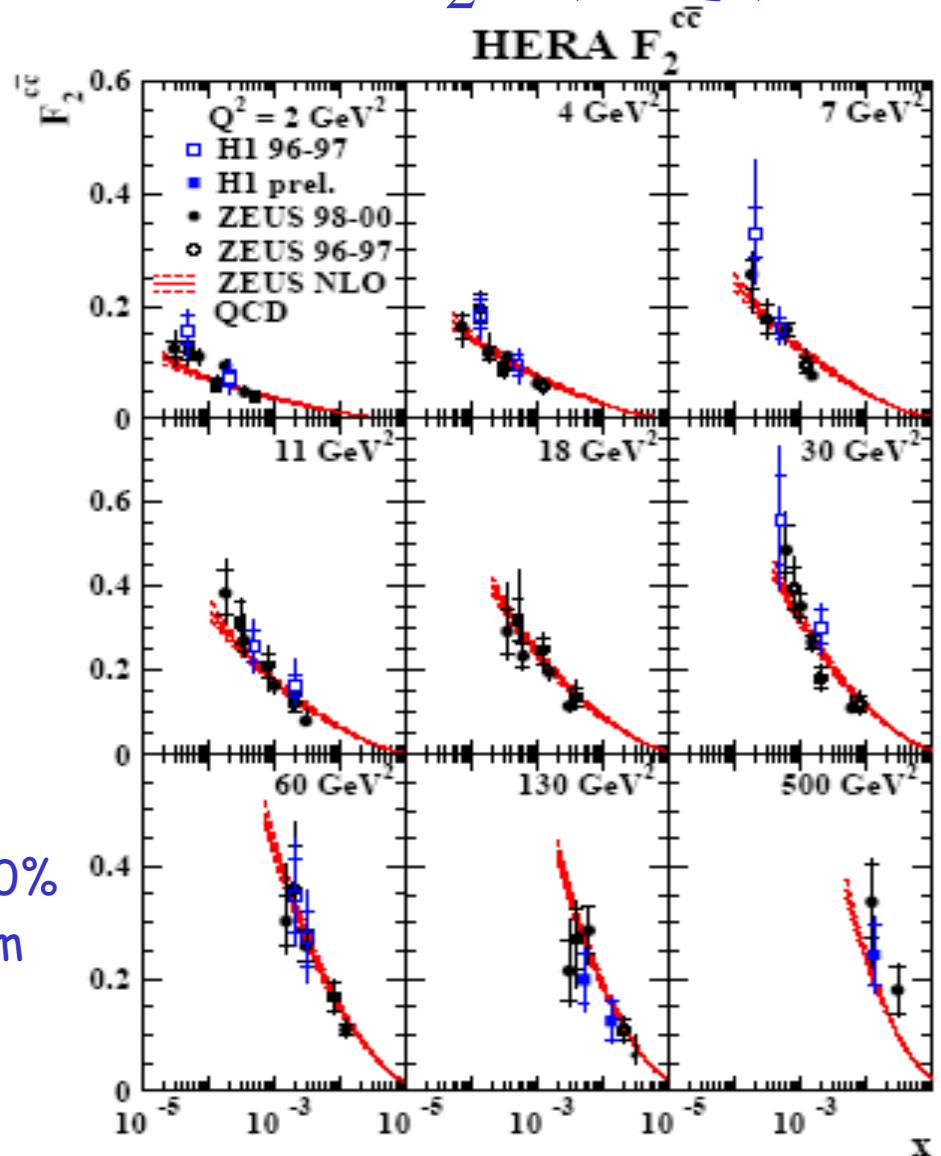
# Charm Structure Function $F_2^{cc} (x, Q^2)$

Boson Gluon Fusion (BGF)



$$D^* \rightarrow D^0 \pi_{slow} \rightarrow K \pi \pi_{slow}$$

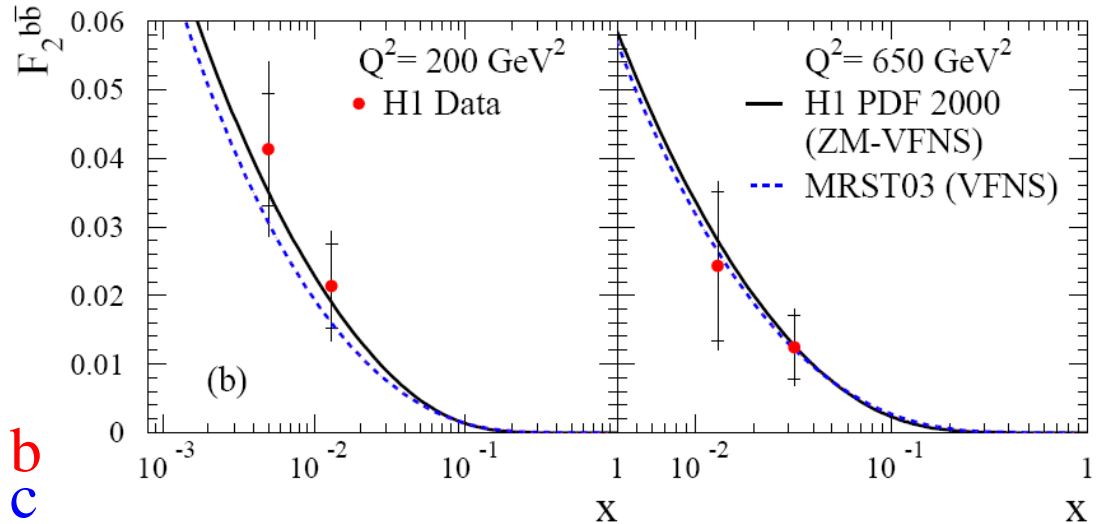
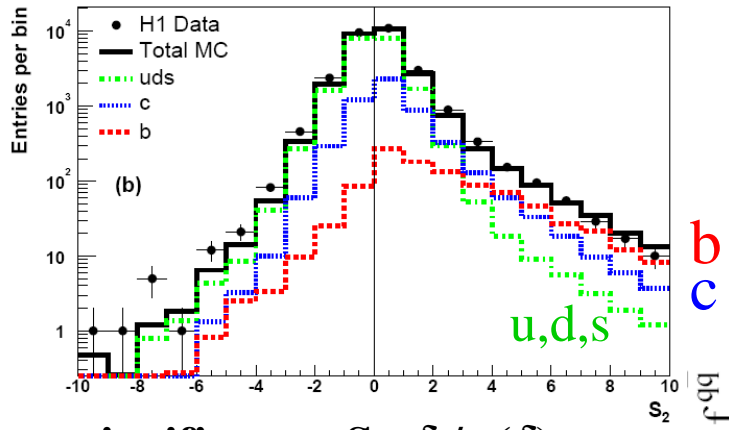
- charm contribution up to 25-30%
- consistent with gluon from scaling violations



# Beauty Structure Function $F_2^{bb}(x, Q^2)$

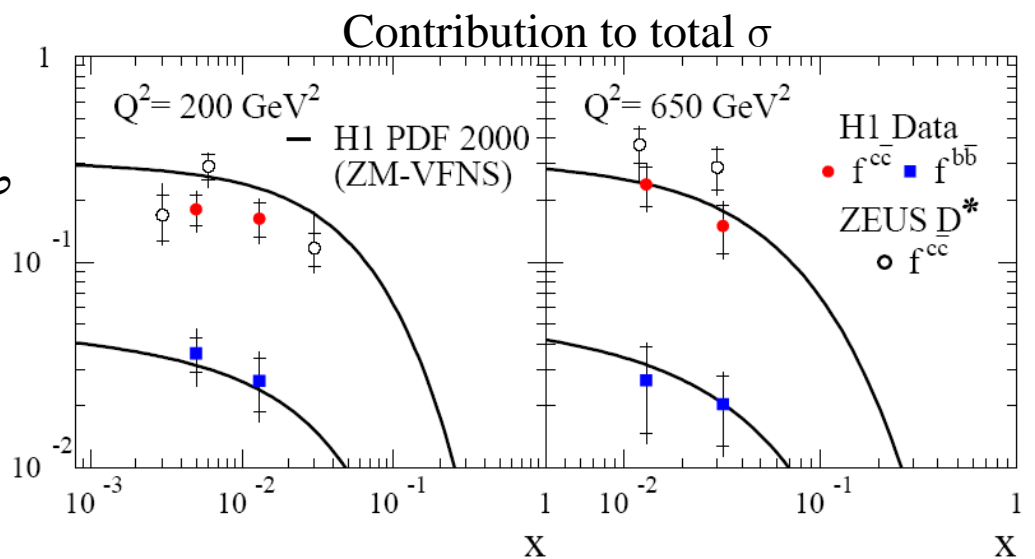
## long lifetimes of b,c hadrons

- use all tracks with  $p_T > 500$  MeV and hits in the H1 silicon tracker
- jet gives b-direction



significance  $S = \delta / \sigma(\delta)$   
 $\delta$  - track impact parameter in  $r-\varphi$

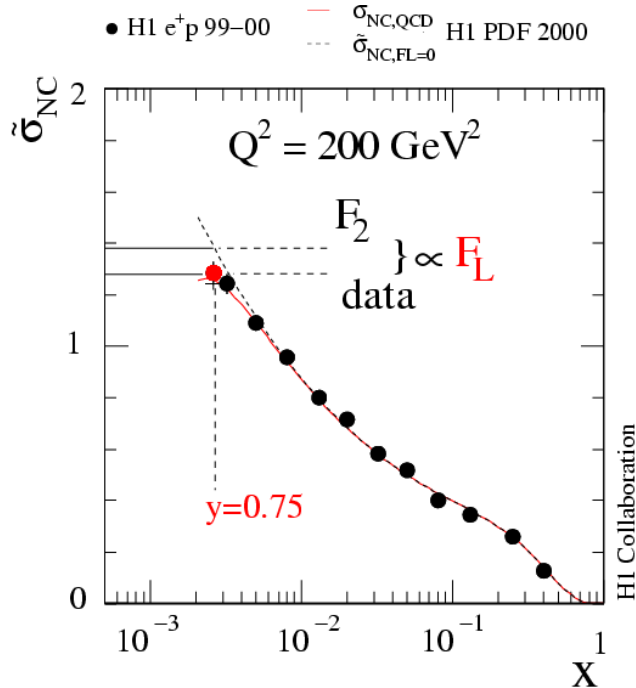
- $F_2^{bb}$  - for the first time
- beauty contribution is  $\sim 3\%$
- consistent with with QCD calculations



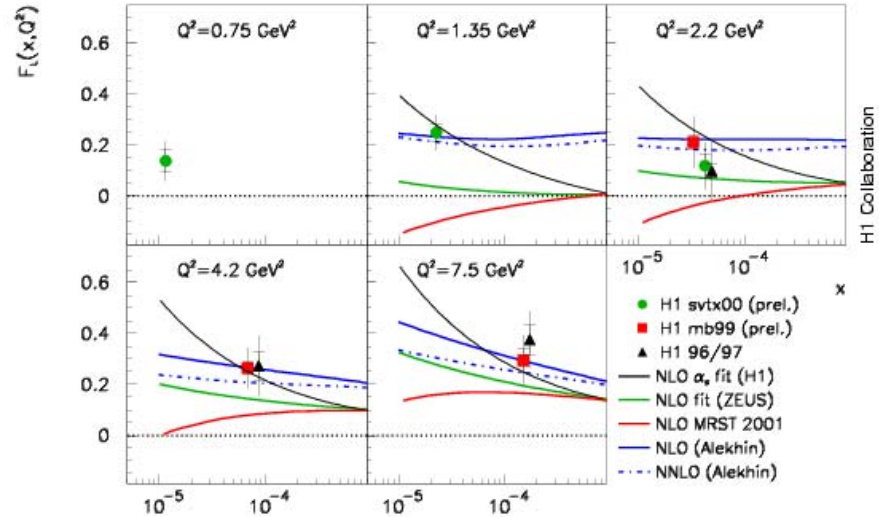


# Determination of $F_L(x, Q^2)$ by H1

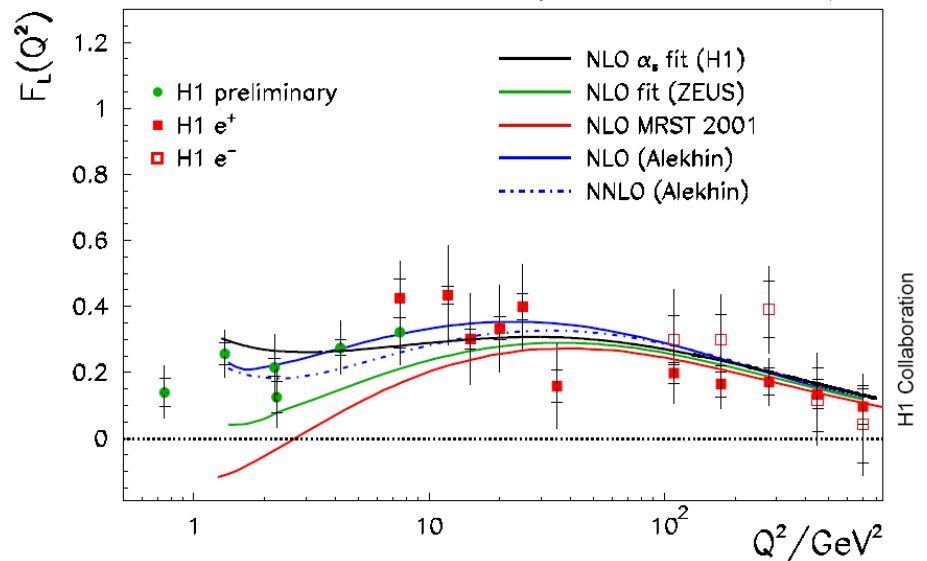
$$F_L = \frac{Y_+}{y^2} (F_2^{QCDfit} - \tilde{\sigma}_{NC})$$



direct  $F_L$  measurements still  
 to be done at HERA  
 → low beam energy running



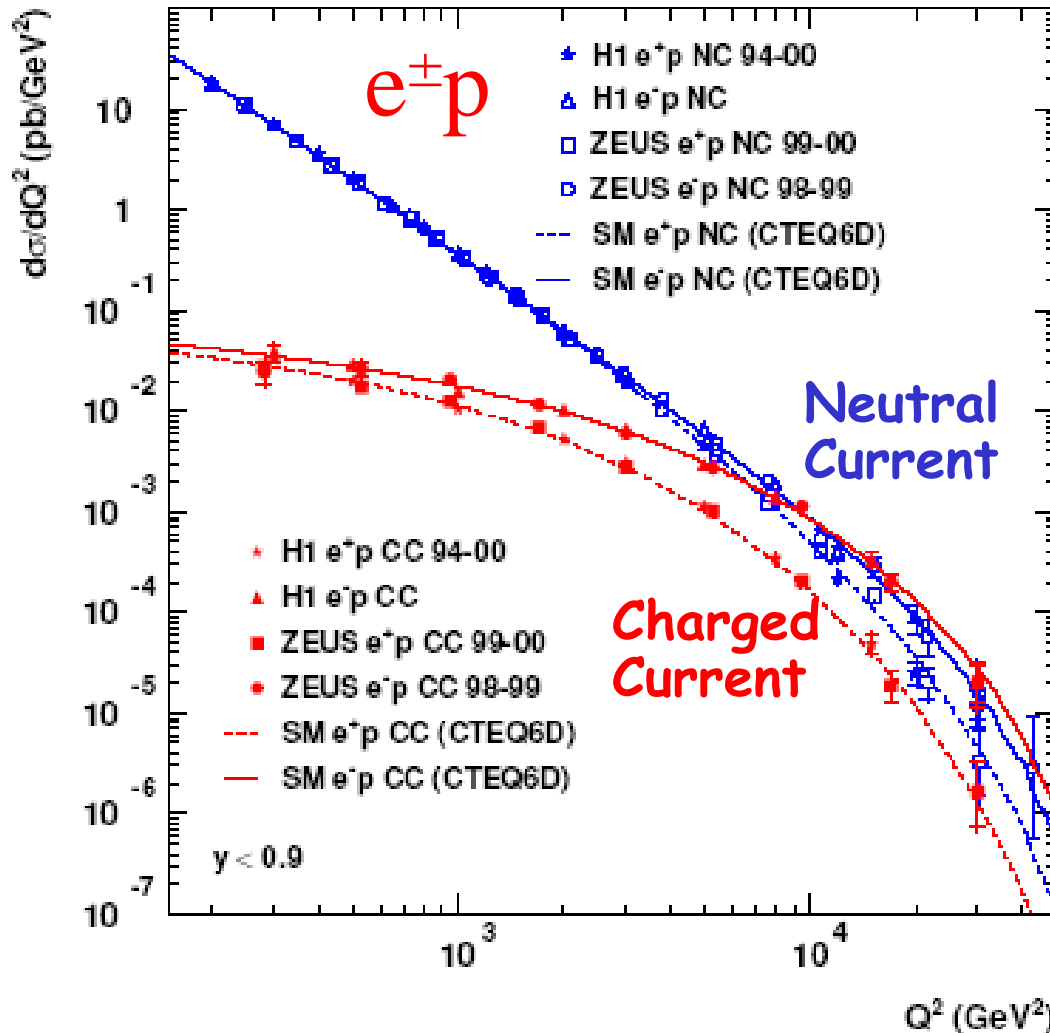
$F_L$  extraction from H1 data (for fixed  $W=276 \text{ GeV}$ )





# NC and CC at High $Q^2$

HERA



quarks are pointlike  
down to proton radius/1000  
 $r < 10^{-18}$  m

$\sigma_{NC} \approx \sigma_{CC}$  at  $Q^2 \approx M_Z^2, M_W^2$   
unification of electromagnetic  
weak interactions

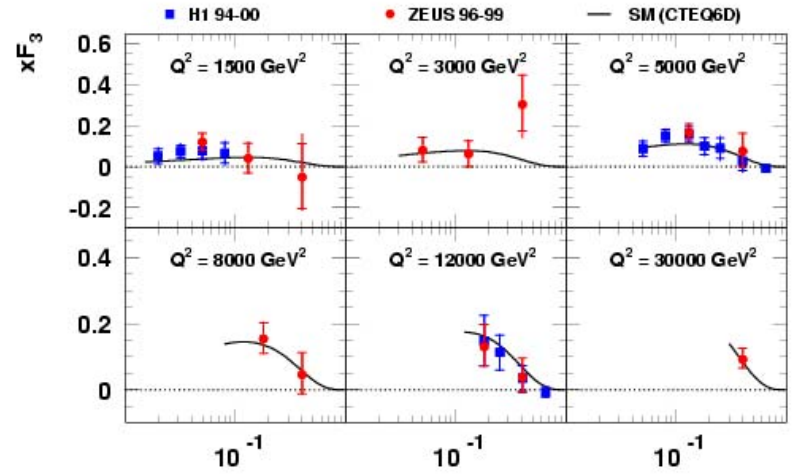
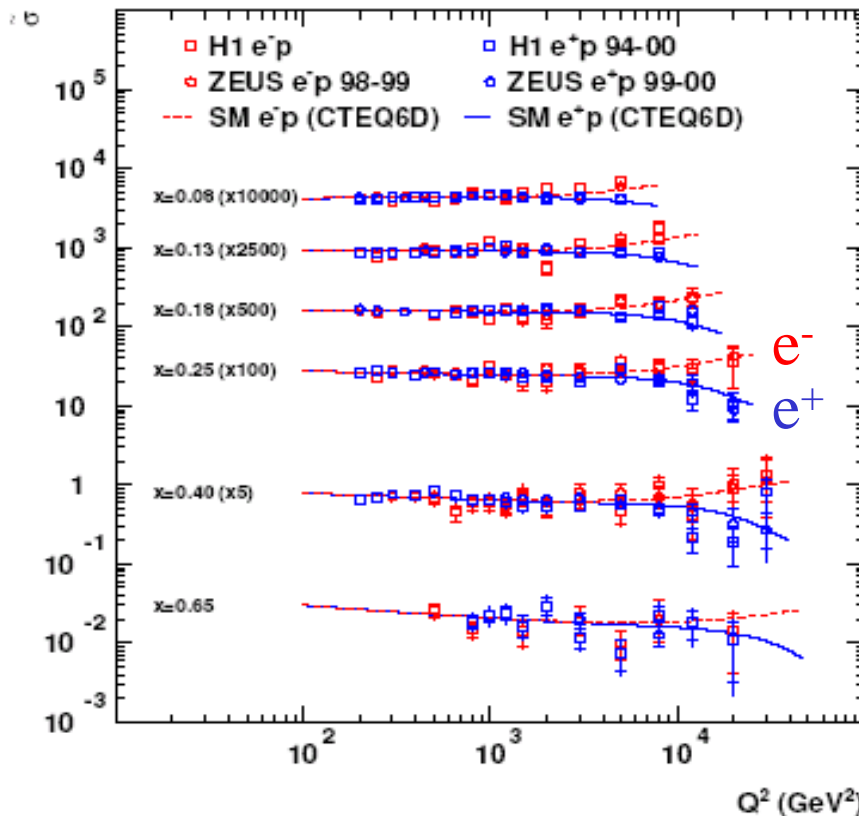
high  $Q^2 \rightarrow$  high  $x$   
provide possibility to unfold  
different quark flavours

# Structure Function $xF_3$ at HERA

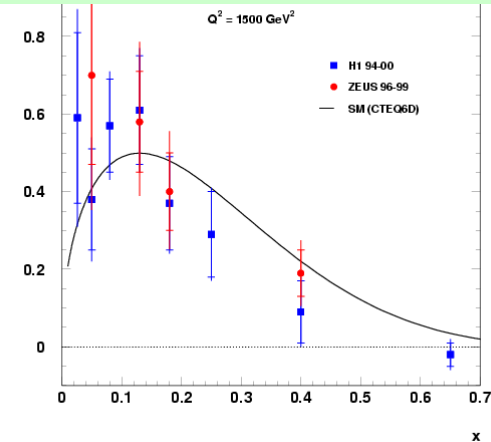
reduced NC cross section:

$$\tilde{\sigma}_{NC}^{\pm} = F_2 - \frac{y^2}{Y_+} F_L \mp \frac{Y_-}{Y_+} xF_3$$

HERA Neutral Current at high  $x$



$$xF_3^{\gamma Z} = \frac{xF_3}{-a_e k_w / (Q^2 + M_Z^2)} \sim 2u_v + d_v$$



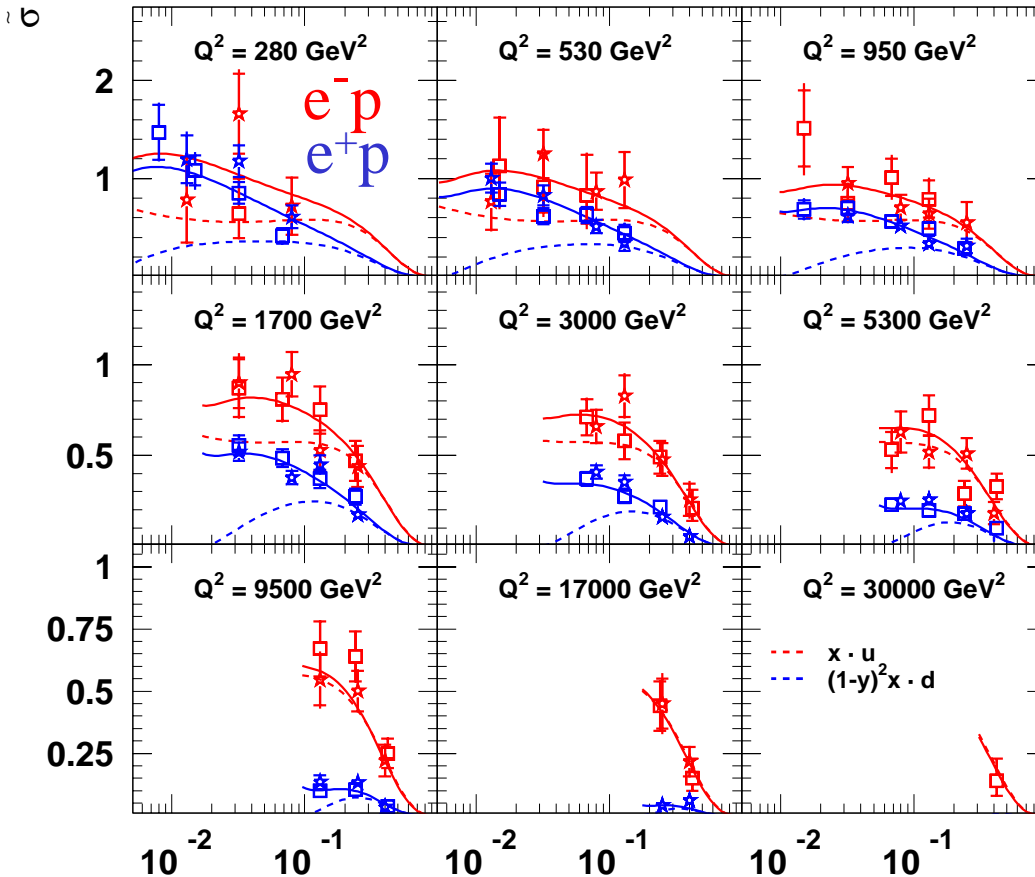
$xF_3$  constrains  $u_v, d_v$  at high  $x$

# Charged Currents

$$\frac{d^2\sigma_{CC}(e^\pm p)}{dx dQ^2} = \frac{G_F^2 M_W^4}{2\pi x} \frac{1}{(Q^2 + M_W^2)^2} \frac{1}{2} \underbrace{[Y_+ W_2 - y^2 W_L \mp Y_- x W_3]}_{\tilde{\sigma}_{CC}(x, Q^2)}$$

- ★ H1 e<sup>-</sup>p
- ★ H1 e<sup>+</sup>p 94-00
- ZEUS e<sup>-</sup>p 98-99
- ZEUS e<sup>+</sup>p 99-00
- SM e<sup>-</sup>p (CTEQ6D)
- SM e<sup>+</sup>p (CTEQ6D)

$\tilde{\sigma}_{CC}(x, Q^2)$  - reduced CC cross section



The CC e<sup>+</sup>p cross section  
- dominated by **d** quark

$$\tilde{\sigma}_{CC}^{e^+p}(x, Q^2) \sim (\bar{u} + \bar{c}) + (1-y)^2(d + s)$$

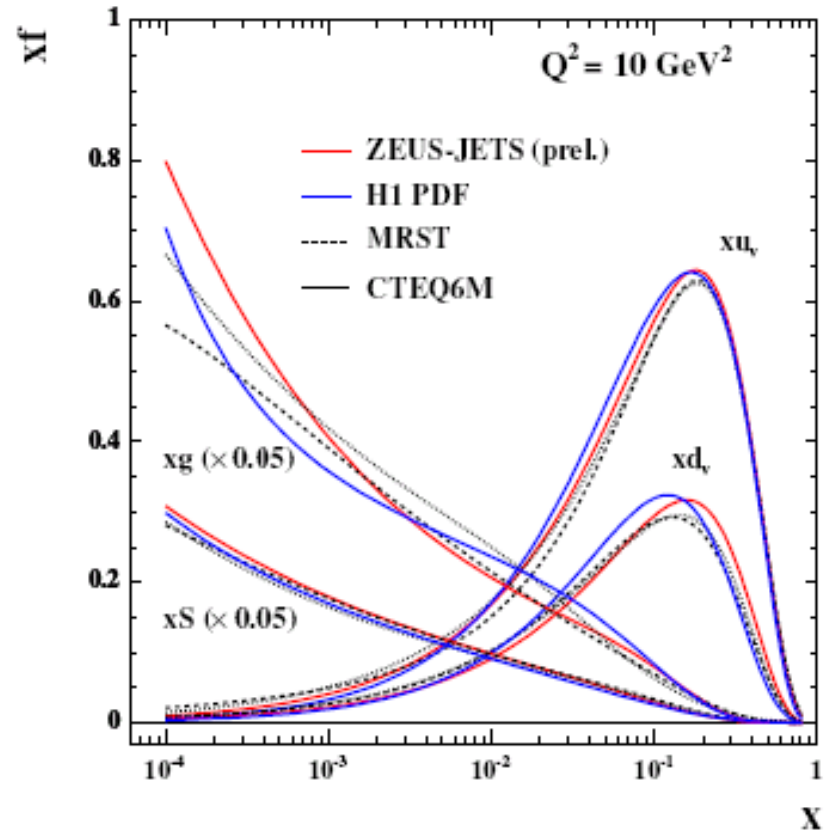
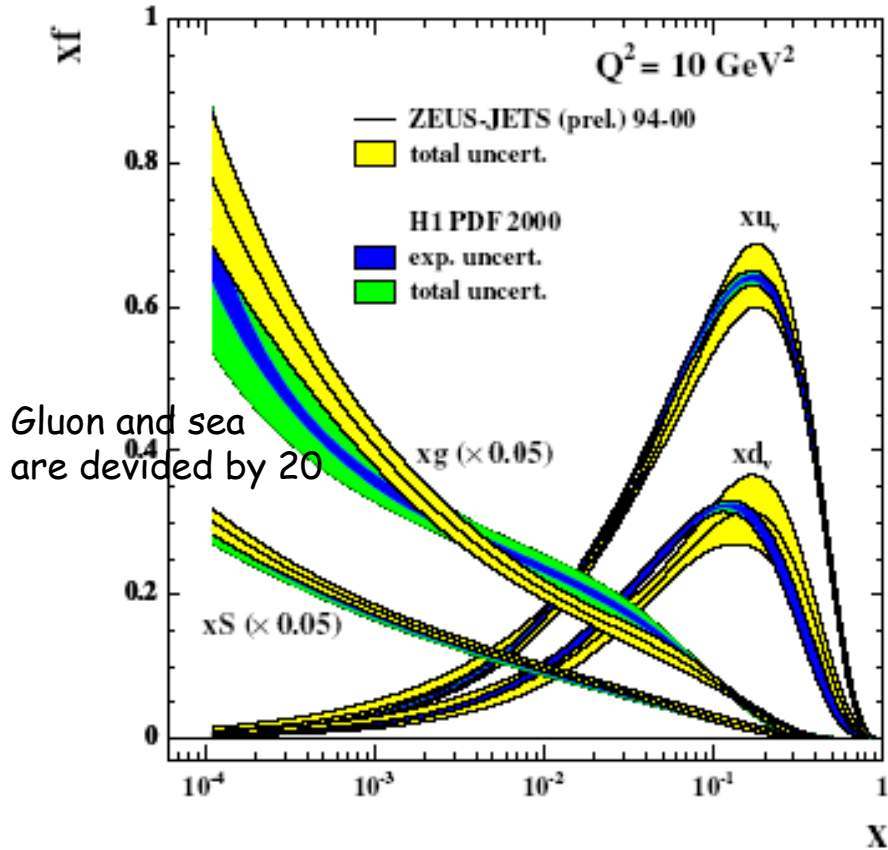
The CC e<sup>-</sup>p cross section  
- dominated by **u** quark

$$\tilde{\sigma}_{CC}^{e^-p}(x, Q^2) \sim (u + c) + (1-y)^2(\bar{d} + \bar{s})$$

CC e<sup>+</sup>p (e<sup>-</sup>p) cross sections  
are suited for constraining  
d (u) quark density

# PDFs from HERA

Parton distributions unfolded using HERA NC and CC data only



- H1 and ZEUS parton distributions are in agreement
- Treatment of systematics, parameterisations forms and other details are subject to conventions

- HERA QCD fits agree with the global fits

H1  $U, \bar{U}, D, \bar{D}, xg \leftrightarrow V, A, xg - \alpha_s$

ZEUS  $u_v, d_v, \bar{u} \pm \bar{d}, xg - \alpha_s$

# First Results from HERA II

**detector and luminosity upgrade**

- efficient data taking since 2003
- $O(1\text{fb}^{-1})$  till 2007

**longitudinally polarised e beam**

**H1** typically  $P_e \sim 50\%$   
rise-time  $\sim 22\text{min}$

Spin Rotator (new)  
**Spin Rotators for the 3 IR's**

**e beam naturally transversely polarized**  
(Sokolov-Ternov effect)

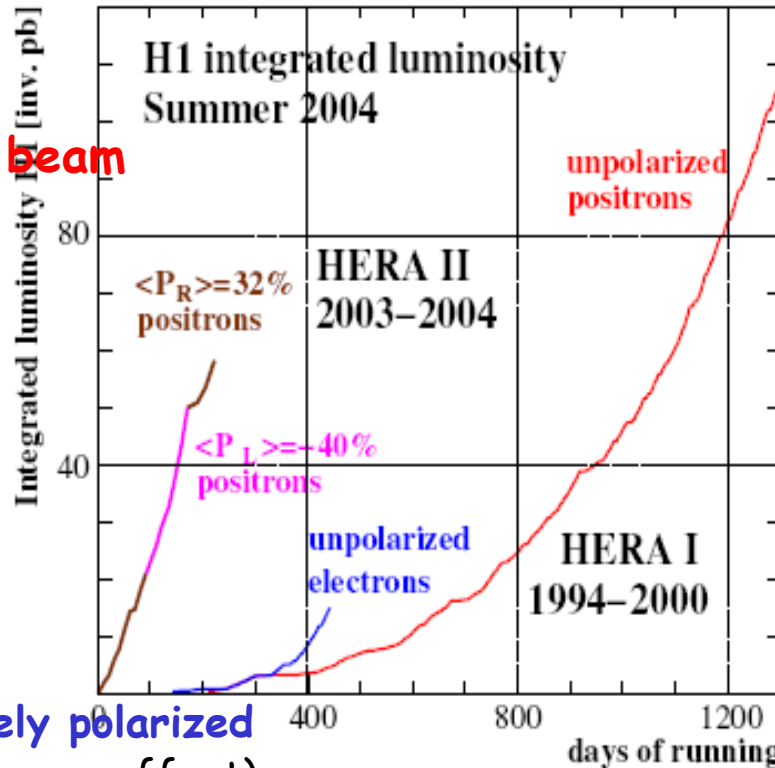
**TPOL**

Spin Rotator (exists)

HERMES

Laser

**LPOL**



$E_e = 27.6 \text{ GeV}$   
 $E_p = 920 \text{ GeV}$

$\sqrt{s} = 319 \text{ GeV}$

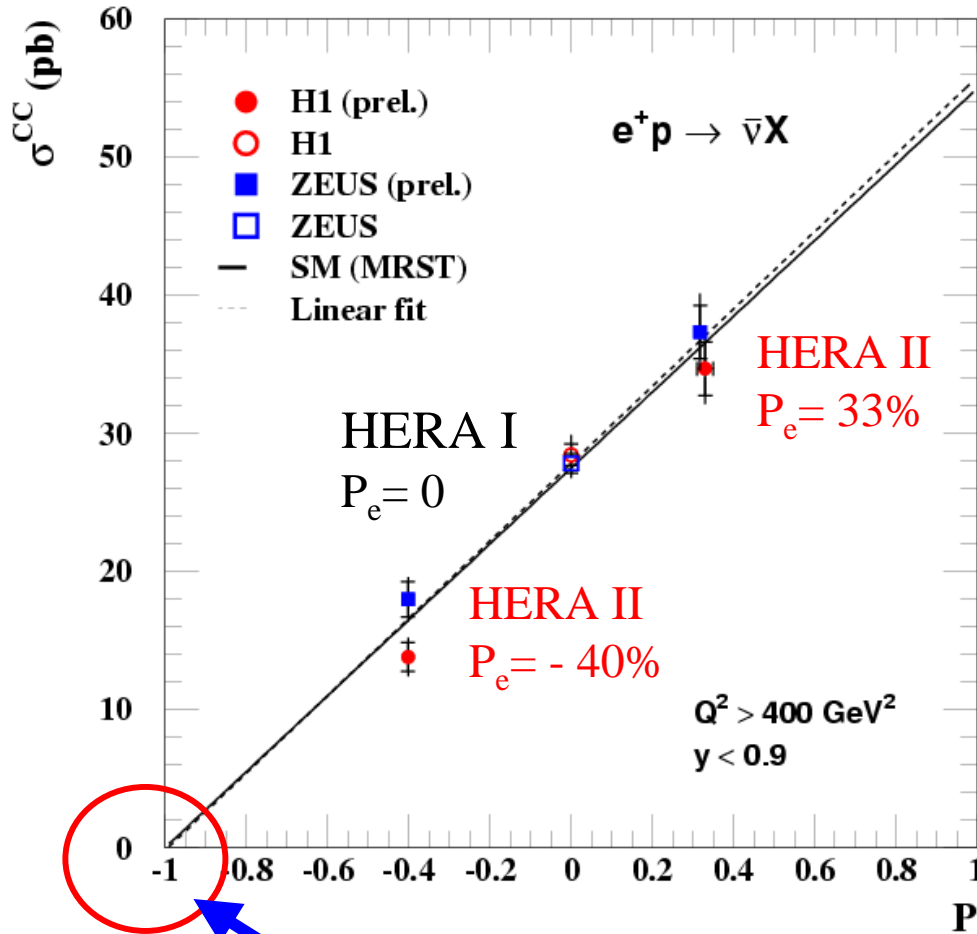
**ZEUS**

electrons

HERA B

# $\sigma_{CC}$ using Longitudinally Polarised $e^+$

## HERA II



$$\sigma_{CC}^{e^+p}(P_e) = (1 \pm P_e) \sigma_{CC}^{e^+p}(P_e = 0)$$

Polarisation dependence is firmly established

Linear fit  $\sigma_{CC} = \alpha + \beta(1 + P_e)$

$$\sigma_{CC}^{tot}(P_e = -1) = -0.2 \pm 1.8(sta) \pm 1.6(sys) pb$$

consistent with

- linear  $(1 + P_e)$  dependence
- intercept of 0

after shutdown fall 2004

→  $e^-$  running

extrapolation to  $P_e = -1$  tests the absence of right-handed current

BARYONS

SF

# Summary

for more than 30 years SF provide a crucial experimental input to establish QPM, QCD and to determine pdfs

still very active area: NuTeV, JLAB, ...

HERA II  $\sim O(1\text{fb}^{-1})$  till 2007, low energy running for  $F_L$

new level of precision (exp.  $\sim 1\%$ , theory NNLO) allows

- to investigate applicability domains for different QCD evolutions
  - to understand high density (low  $x$ ) QCD
  - to provide information essential for future LHC collider
- see HERA-LHC workshop: <http://www.desy.de/~heralhc/>

large potential for the long term future

- HERA III (ed, ...), eRHIC, e(ILC) $\times$ p(HERA,TeVatron)

# Strange Sea Asymmetry Results from NuTeV

the "NuTeV Anomaly"  $R^- = \frac{\sigma_\nu^{NC} - \sigma_{\bar{\nu}}^{NC}}{\sigma_\nu^{CC} - \sigma_{\bar{\nu}}^{CC}} \simeq \frac{1}{2} - \sin^2 \Theta_W$

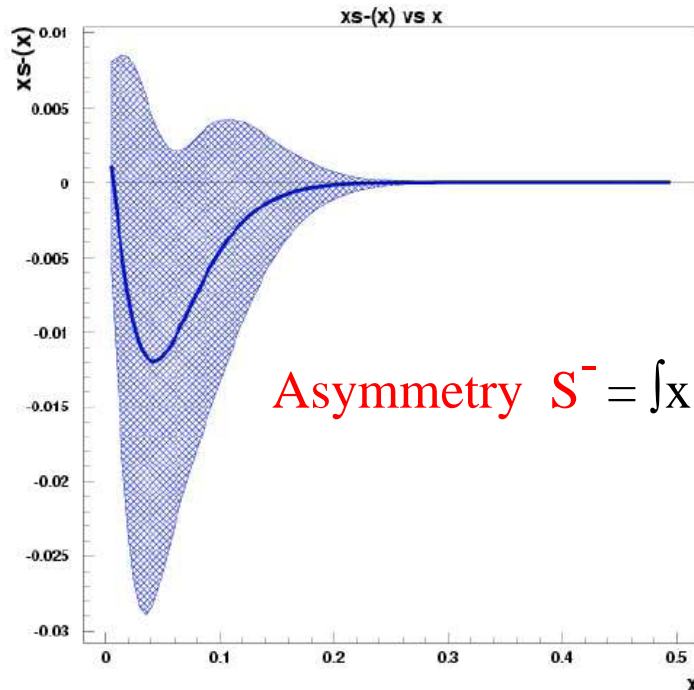
a 3.1  $\sigma$  discrepancy:

NuTeV  $\sin^2 \Theta_W = 0.2277 \pm 0.0016$

LEP EWVG  $\sin^2 \Theta_W = 0.2227 \pm 0.0037$

Test one of the interpretations (from many):

- strange/anti-strange sea quark asymmetry



Asymmetry  $S^- = \int xs^- dx = \int x[s(x) - \bar{s}(x)] dx = -0.0009 \pm 0.0014$

*dimuon production:*

$\nu_\mu s \rightarrow \mu^- c \rightarrow \mu^- \mu^+ X$  (CCFR, NuTeV)

NLO fits to  $\nu$  and  $\bar{\nu}$  dimuon data

To explain "NuTeV Anomaly"  
would require  $S^- = +0.0060$